

# Performance Improvement of Calculation of Static Magnetic Field of Micromagnetic Simulator Using Supercomputer FX10

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## Background

Micromagnetic simulator is used for analyzing dynamic behavior of magnetization. However, calculation of static magnetic fields among a huge number of small nanosized cells, into which simulation model discretizes simulated field, is time consuming.

## Purpose

We used the supercomputer FX10 at the University of Tokyo to investigate possibility of using parallelizing methods to decrease calculation time.

- Parallelization of the message passing interface (MPI) with MPI\_Allgather() for CPU-to-CPU communications with various directions of parallelization in its three-dimensional (3-D) model.
- Comparing three parallelizing methods for communication among CPUs, namely MPI, multithread parallelization with OpenMP, and Open MP/MPI hybrid parallelization.

## Calculation methods

Landau-Lifshitz-Gilbert equation

$$(1 + \alpha^2) \frac{d\vec{M}}{dt} = -\gamma \vec{M} \times (\vec{H}_{eff} - \alpha \vec{H}_{st}) - \frac{\gamma}{M_s} \vec{M} \times \{ \vec{M} \times (\alpha \vec{H}_{eff} + \vec{H}_{st}) \}$$

$\vec{M}$  : magnetization vector  $t$  : time

$\gamma$  : gyro magnetic constant  $\alpha$  : damping constant

$\vec{H}_{eff}$  : effective field vector (sum of external, anisotropy, exchange, and static field)  $\vec{H}_{st}$  : spin-torque field vector

Static magnetic field equation

$$\begin{bmatrix} H_x \\ H_y \\ H_z \end{bmatrix} = \sum_{cell} \begin{bmatrix} S_{xx} & S_{xy} & S_{xz} \\ S_{yx} & S_{yy} & S_{yz} \\ S_{zx} & S_{zy} & S_{zz} \end{bmatrix} \cdot \begin{bmatrix} M_x \\ M_y \\ M_z \end{bmatrix}$$

$H_a(a:x, y, z)$  : static magnetic field

$S_{ab}(b:x, y, z)$  : structure factor depending on shape of cell and distance of cell-to-cell

$M_a$  : magnetization

↓ FFT(Fast Fourier Transform)

$$H(k) = S(k) \cdot M(k)$$

$H(k)$  : static magnetic field  $S(k)$  : structure factor

$M(k)$  : magnetization  $k$  : frequency

FFT in X and Y directions are sequentially performed.

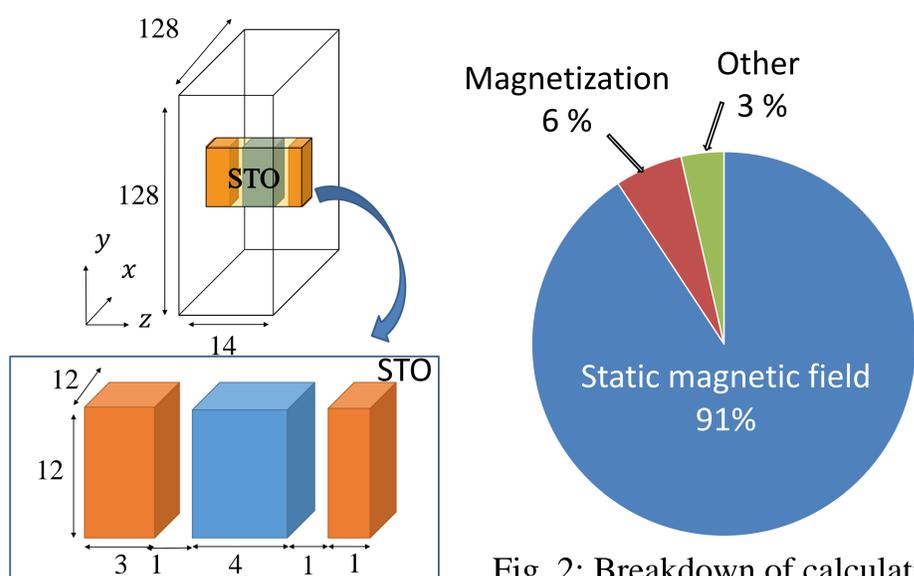


Fig. 2: Breakdown of calculation time in LLG simulator.

Subscript of 3-D array is [i][j][k], elements of [i], [j], and [k] are termed the first, second and third elements, respectively.

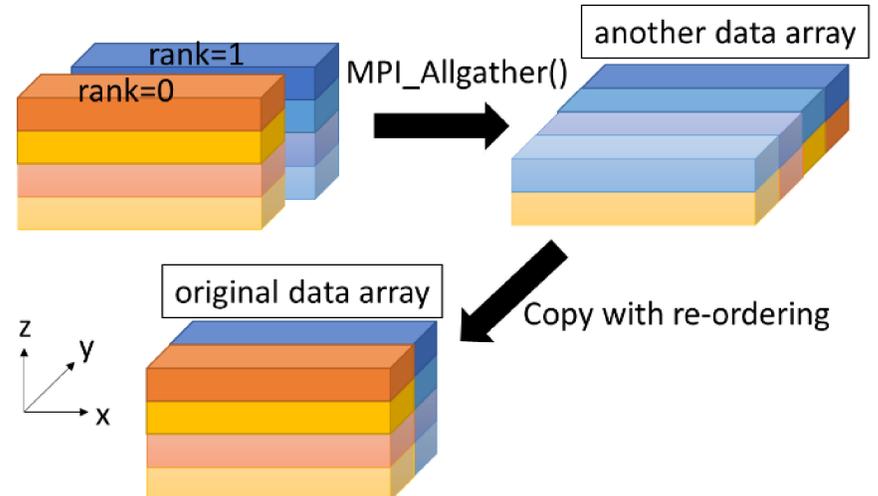


Fig. 3: Schematic of data array for MPI parallelization in second and third element using MPI\_Allgather().

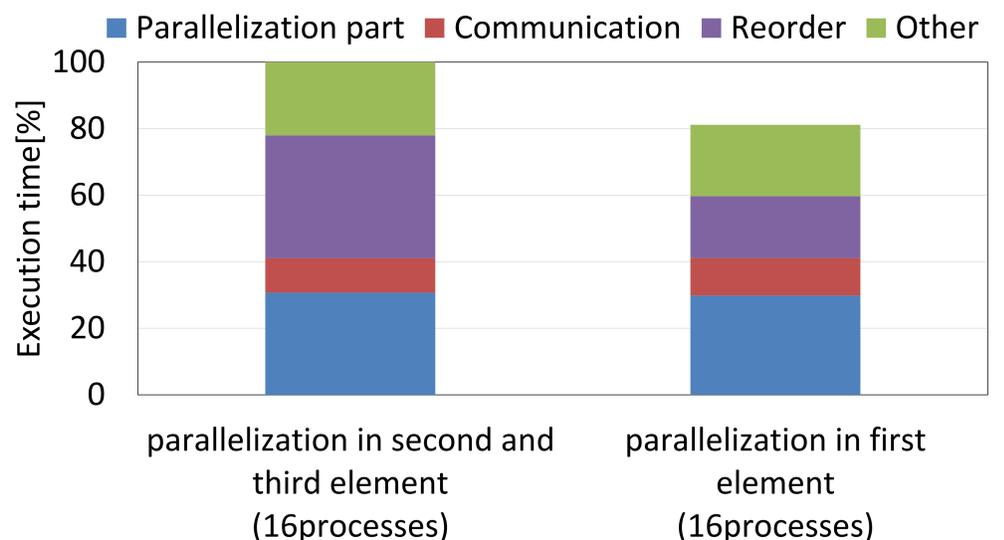


Fig. 4: Comparison between conventional and improvement methods in breakdown of execution time in MPI\_Allgather().

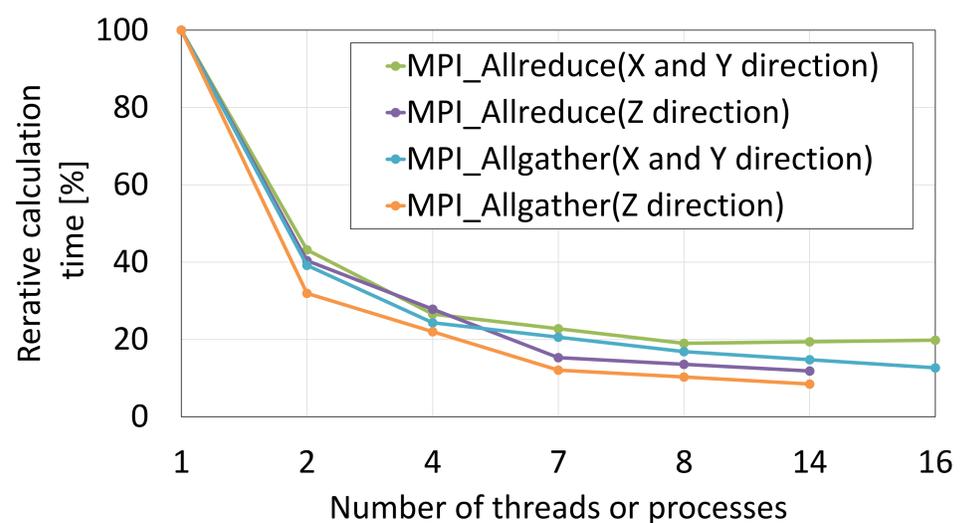


Fig. 5: Relationship between number of processes and calculation time in MPI.

## Conclusions

- Parallelization in Z-direction is faster than those in the X- and Y-directions.
- Calculation time can be decreased by parallelizing the first element of data array.
- Calculation time can be reduced by applying hybrid parallelization using MPI with MPI\_Allgather() in Z-direction (without FFT) and OpenMP in X- and Y-directions (with FFT for static magnetic field and magnetization).

## ACKNOWLEDGMENTS

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